

Simplification with Karnaugh Maps

Part A For the Karnaugh map below, circle the prime implicants. Then list each product term derived from the map indicating which are essential. You won't necessarily need all lines.

	\overline{B}	B				
	⏟	⏟				
\overline{A}	1	1	1	1	\overline{C}	
A	0	1	1	0	C	
\overline{A}	1	1	0	0	\overline{C}	
A	1	1	1	1	C	
	⏟	⏟	⏟			
	\overline{D}	D	\overline{D}			

	prime implicant	essential?
	\overline{C}	yes <input checked="" type="checkbox"/> no <input type="checkbox"/>
	$\overline{B} D$	yes <input type="checkbox"/> no <input checked="" type="checkbox"/>
	$A \overline{B}$	yes <input checked="" type="checkbox"/> no <input type="checkbox"/>
	$\overline{A} D$	yes <input checked="" type="checkbox"/> no <input type="checkbox"/>
		yes <input type="checkbox"/> no <input type="checkbox"/>
		yes <input type="checkbox"/> no <input type="checkbox"/>
		yes <input type="checkbox"/> no <input type="checkbox"/>

Part B Write the simplified sum of products expression for this Karnaugh map.

$$F_{(A,B,C,D)} = \overline{C} + A\overline{B} + \overline{A}D$$

Part C Write the simplified product of sums expression for this Karnaugh map.

$$F_{(A,B,C,D)} = (\overline{A} + \overline{B} + \overline{C})(A + \overline{C} + D)$$