## Arithmetic Units

Part A Complete the truth table for a one bit binary full-adder.

| $X$ | $Y$ | $C A R R Y_{\text {in }}$ | SUM | CARRY out |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 |  |  |
| 1 | 0 | 0 |  |  |
| 0 | 1 | 0 |  |  |
| 1 | 1 | 0 |  |  |
| 0 | 0 | 1 |  |  |
| 1 | 0 | 1 |  |  |
| 0 | 1 | 1 |  |  |
| 1 | 1 | 1 |  |  |
|  |  |  |  |  |

Part B Implement a one bit binary full-adder using AND, OR, NAND, NOR, NOT, XOR, and XNOR gates. Label the inputs $A, B$, and $C A R R Y_{i n}$. Label the outputs $S U M$ and $C A R R Y_{\text {out }}$. Use mixed logic design methodology.

Part C The truth table for a one bit binary full-subtractor is given below. First determine the simplified expression for DIFFERENCE and BORROW ${ }_{\text {out }}$. Then implement this truth table using basic gates (AND, OR, NAND, NOR, NOT, XOR, and XNOR). Be sure to label the inputs $X, Y, B O R R O W_{i n}$, and the outputs DIFFERENCE, and BORROW $W_{\text {out }}$. Assume that you have the input signals and their complements.

| $X$ | $Y$ | BORROW $_{\text {in }}$ | DIFFERENCE | BORROW $_{\text {out }}$ |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 0 | 1 | 0 |
| 0 | 1 | 0 | 1 | 1 |
| 1 | 1 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 | 1 |
| 1 | 0 | 1 | 0 | 0 |
| 0 | 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 | 1 |

DIFFERENCE = $\qquad$
BORROW ${ }_{\text {out }}=$ $\qquad$
Part $\mathbf{D}$ Using a four bit adder, build a four bit adder/subtractors. Use AND, OR, NAND, NOR, NOT, XOR, and XNOR gates plus the adder drawn below. Label your inputs $X_{3}, X_{2}, X_{1}, X_{0}, Y_{3}, Y_{2}, Y_{1}, Y_{0}$, and $\overline{A d d} /$ Subtract. Label your outputs $Z_{3}, Z_{2}, Z_{1}$, and $Z_{0}$.


