## Expression Simplification

Part A Complete the truth table for the following expression:
Out $=\bar{A} C D+\bar{A} \bar{B} \bar{D}+\bar{A} \bar{B} \bar{C} D+B C D+\bar{A} B C+A B C \bar{D}$

| $D$ | $C$ | $B$ | $A$ | OUT |
| :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 |  |
| 0 | 0 | 0 | 1 |  |
| 0 | 0 | 1 | 0 |  |
| 0 | 0 | 1 | 1 |  |
| 0 | 1 | 0 | 0 |  |
| 0 | 1 | 0 | 1 |  |
| 0 | 1 | 1 | 0 |  |
| 0 | 1 | 1 | 1 |  |


| $D$ | $C$ | $B$ | $A$ | $O U T$ |
| :--- | :--- | :--- | :--- | :--- |
| 1 | 0 | 0 | 0 |  |
| 1 | 0 | 0 | 1 |  |
| 1 | 0 | 1 | 0 |  |
| 1 | 0 | 1 | 1 |  |
| 1 | 1 | 0 | 0 |  |
| 1 | 1 | 0 | 1 |  |
| 1 | 1 | 1 | 0 |  |
| 1 | 1 | 1 | 1 |  |

Part B For this expression, (A) express the minterm sum of products equation, and (B) express the maxterm product of sums equation.
(A) $\operatorname{SOP}$ (minterms) $=$ $\qquad$
(B) $\operatorname{POS}($ maxterms $)=$ $\qquad$

Part C Determine a simplified expression for the original expression above using a Karnaugh Map. Circle and list the prime implicants, indicating which are essential. Then write the simplified expression.



$O u t=$ $\qquad$

