ECE2020 Final Exam Summer 2013 GTL
July 31, 2013
Name: $\qquad$

Show your work for any possible partial credit. 100 possible points, 12 exam pages plus a figure.

| High Level Language |  |  |
| :---: | :---: | :---: |
| Assembly Language |  |  |
| Instruction Set |  |  |
| Memory | Data Path | Controller |
| Storage | Functional |  |
| Units | State <br> Machines |  |
| Building Blocks |  |  |
| Gwitches and Wires |  |  |

1) (6 Points) Three incomplete circuits are shown below. Complete each circuit by adding the needed switching network so the output is pulled high or low for all combinations of inputs (i.e., no floats or shorts). Complete each circuit (pull down, pull up, or both) and write the expression if one is not given. Assume both inputs and complements are available.


Out $_{1}=$ $\qquad$ $\mathrm{Out}_{2}=$ $\qquad$ $\mathrm{Out}_{3}=\overline{\mathrm{D}}(\overline{\mathrm{A}}+\mathrm{B}+\overline{\mathrm{C}}) \mathrm{E}$

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2) (5 points) Implement the following expression using only NOR gates and inverters. Then determine the number of switches required. Use proper mixed logic notation. Do not modify the expression. Do not assume compliments of inputs are available.

Out $=((\overline{\bar{A} \cdot \bar{B}+\mathrm{C})} \bar{D}+\mathrm{E}) \bar{F}$

Number of switches $\qquad$

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| Gate |  |  |
| Switches and Wires |  |  |


3) (5 points) Using only the devices below, implement a two-to-one mux on the diagram below. (The block diagram of a 2 to 1 mux is show above just as an FYI only).

In0 -

$-\infty-$ - Out
In1 -


## Select -

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| Building Blocks |  |  |
| Gwate |  |  |


4) (5 points) Using a two-to-one mux, implement a transparent latch using basic gates (NAND, NOR, AND, OR, NOT, pass). Enable here is an active high write enable. (The block diagram of a transparent latch is show above just as an FYI only).

Try to minimize transistors.


- Output


## Enable

| High Level Language |  |  |
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| Gate |  |  |
|  |  |  |

5) (8 points) Consider the register implementation below.


Assume the following signals are applied to the register above. Draw the signal at point A (output of the first latch), the signal at point OUT (output of second latch). Assume A and OUT start at logic unknown values.


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6) a)(5 points) Complete the truth table below to the left for a "full adder" as shown below on the right.

b) (10 Points) Using four of the full adder blocks shown above to the right, show how four of them would be used to implement a four bit adder that would be able to add/subtract two four bit numbers. Your inputs are X3, X2, X1, X0, Y3, Y2, Y1, Y0, a $\overline{d d} /$ sub, and your outputs include S3, S2, S1, S0. You may use any additional logic gate types you want. Draw your hardware diagram below:

## 7) ( 10 points total) State machine problem straight from the practice problems:

## Strike State Machine

You're designing a baseball scoreboard. A sub-problem involves keeping track of strikes and fouls. A strike occurs when the batter swings at the ball and misses, or when the batter does not swing at a "good" pitch. If a batter earns three strikes during his/her turn at bat, he/she is "out" . A foul occurs when the batter hits the ball, but the ball does not land in "fair" territory. Fouls are counted as strikes until the batter earns two strikes. Then fouls are ignored. The state diagram below captures these rules. The null input indicates neither a strike nor a foul occurred during that clock cycle. The strike and foul input cannot occur simultaneously, so the output for this case is don't care.


Part A Using the state diagram above, complete the state table for this diagram. The inputs are strike, foul, and state bits $S_{1}$ and $S_{0}$. The outputs are next state bits $N S_{1}$ and $N S_{0}$, and out.

| $S_{1}$ | $S_{0}$ | strike | foul | $N S_{1}$ | $N S_{0}$ | out |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 |  |  |  |
| 0 | 0 | 0 | 1 |  |  |  |
| 0 | 0 | 1 | 0 |  |  |  |
| 0 | 1 | 0 | 0 |  |  |  |
| 0 | 1 | 0 | 1 |  |  |  |
| 0 | 1 | 1 | 0 |  |  |  |
| 1 | 0 | 0 | 0 |  |  |  |
| 1 | 0 | 0 | 1 |  |  |  |
| 1 | 0 | 1 | 0 |  |  |  |

Part B Determine the simplified logical expression for $N S_{1}, N S_{0}$, and out using your state table in part A. Complete the Karnaugh maps below, identify the prime implicants, and express the result.

$N S_{1}=$ $\qquad$
$N S_{0}=$ $\qquad$
out $=$ $\qquad$
Part C Implement this state machine using your expression from part B, plus two register cells. Use an icon for a one bit register cell. You do not have to show the implementation of a register here. Your logic should be simplified.

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8) (6 points) SIMM Memory System:

Using SIMMs that are 8 million addresses by 8 bit words:
Part A Suppose that these SIMMS are used to build a 16 million address memory system with 8 bit words. Using however many of these SIMMs you need, draw this memory system. In the drawing you make below, add as many SIMM chips as you need and then be sure you label the memory system inputs, Addr, R/W, and Mem Sel, and the system's outputs D0, D1, D2, etc. Also label bus widths, and inputs and outputs of any required decoders. Put a star on the chip(s) containing the memory location addressed by an address containing a one followed all zeros (all of the address bits are input as a zero except the most significant bit which is a one).


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9) Using the attached single cycle datapath we have discussed extensively in class (see last page of exam for part of it), implement the microcode for the following instructions (see instruction examples also on last page):
a) (5 points) addi $\$ 3$, $\$ 2,25$

| $\#$ | X | Y | Z | rw <br> e | im <br> en | im va | au <br> en | -a <br> /s | lu <br> en | lf | su <br> en | st | ld <br> en <br> en | st <br> en | r/ <br> -w | msel | description |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

b) (5 points)
sw \$1, (\$2)

| $\#$ | X | Y | Z <br> rw <br> e | im <br> en | im va | au <br> en | -a <br> /s | lu <br> en | lf | su <br> en | st | ld <br> en <br> en | st <br> en | r/ <br> -w | msel | description |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

c) (5 points) Thinking about the "putting it all together" system block diagram: Which bit fields in the part (a) microcode you wrote above would be stored in a Read Only Memory controller? For those fields not stored in the Read Only memory controller where would they come from?

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10) ( 5 points) Instruction Format. For the third instruction type we discussed, the Immediate Instruction Format, show the actual 32 bits for the instruction:
addi $\$ 10, \$ 8,4$
assuming the opcode for addi is 001000 .
$--------------------------------$
11) Assembly language programming

Consider the following MIPS program fragment. The attached last exam page lists the instruction set and explains them with examples.

| address | label | instruction |
| :--- | :--- | :--- |
| 1000 | start: | addi $\$ 1, \$ 0,300$ |
| 1004 |  | lw $\$ 2,(\$ 1)$ |
| 1008 | loop: | addi $\$ 1, \$ 1,4$ |
| 1012 |  | lw $\$ 4,(\$ 1)$ |
| 1016 |  | slt $\$ 3, \$ 2, \$ 4$ |
| 1020 |  | beq $\$ 3, \$ 0$, skip1 |
| 1024 |  | add $\$ 2, \$ 0, \$ 4$ |
| 1028 | skip1: | slti $\$ 3, \$ 1,324$ |
| 1032 |  | bne $\$ 3, \$ 0,100 p$ |
| 1036 |  | add $\$ 5, \$ 0, \$ 2$ |

Assume memory holds the following starting at address 300:

| Address | Data |
| :---: | :---: |
| 300 | -16 |
| 304 | -7 |
| 308 | -12 |
| 312 | 5 |
| 316 | 8 |
| 320 | -3 |
| 324 | 10 |
| 328 | -19 |
| 332 | 34 |
| 336 | 20 |

Part a) (5 points) How many words of data are read in by the program fragment?
Total number of data words read:

Part b) (5 points) How many times is the add instruction at address 1024 executed?
Number of times:

Part c) (5 points) What are the values in the following registers at the end of the program fragment?
\$1 =
\$2 =
\$3 =
\$4 =
\$5 =
Part d) (5 points) What does this program fragment do?

You may tear this off from the exam and you do not need to turn in this page.
 $-16$


| instruction | example | meaning |
| :---: | :---: | :---: |
| add | add \$1,\$2,\$3 | \$1 = \$2 + \$3 |
| subtract | sub \$1, \$2, \$3 | \$1 = \$2 - \$3 |
| add immediate | addi \$1,\$2,100 | \$1 = \$2 + 100 |
| multiply | mul \$1,\$2,\$3 | \$1 = \$2 * \$3 |
| divide | div \$1,\$2,\$3 | \$1 = \$2 / \$3 |
| and | and \$1,\$2,\$3 | \$1 = \$2 \& \$3 |
| or | or \$1,\$2,\$3 | \$1 = \$2 \| \$3 |
| xor | xor \$1,\$2,\$3 | \$1 = \$2 xor \$3 |
| and immediate | andi \$1,\$2,100 | \$1 = \$2 \& 100 |
| or immediate | ori \$1,\$2,100 | \$1 = \$2 \| 100 |
| xor immediate | xori \$1,\$2,100 | \$1 $=\$ 2$ xor 100 |
| shift left logical | sll \$1,\$2,5 | \$1 = \$2 << 5 (logical) |
| shift right logical | srl \$1,\$2,5 | \$1 = \$2 >> 5 (logical) |
| shift left arithmetic | sla \$1,\$2,5 | \$1 $=$ \$2 << 5 (arithmetic) |
| shift right arithmetic | sra \$1,\$2,5 | \$1 = \$2 >> 5 (arithmetic) |
| load word | lw \$1, (\$2) | \$1 = memory [\$2] |
| store word | sw \$1, (\$2) | memory [\$2] = \$1 |
| load upper immediate | lui \$1,100 | \$1 $=100 \times 2^{16}$ |
| branch if equal | beq \$1,\$2,100 | if $(\$ 1=\$ 2), \mathrm{PC}=\mathrm{PC}+4+(100 * 4)$ |
| branch if not equal | bne \$1, \$2,100 | if (\$1 $\ddagger$ \$2), $\mathrm{PC}=\mathrm{PC}+4+(100 * 4)$ |
| set if less than | slt \$1, \$2, \$3 | if (\$2< \$3), \$1 = 1 else \$1 = 0 |
| set if less than immediate | slti \$1, \$2, 100 | if (\$2<100), \$1 = 1 else \$1 = 0 |
| jump | j 10000 | $\mathrm{PC}=10000 * 4$ |
| jump register | jr \$31 | $\mathrm{PC}=\$ 31$ |
| jump and link | jal 10000 | \$31 = PC + 4; PC = 10000*4 |

