Problem 1 (3 parts, 24 points)
Decoding Decoders
Part A ( 6 points) Define a 1 to 2 decoder by completing the behavior table.

| IN | EN | O0 | O1 |
| :---: | :---: | :---: | :---: |
| $X$ | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 |
| 1 | 1 | 0 | 1 |



Part B (8 points) Implement a 1 to 2 decoder using basic gates. Assume only true (noncomplemented) inputs are available. Label all inputs and outputs.


Part C (10 points) Using only the three 1 to 2 decoders shown below, implement a 2 to 4 decoder with an enable. Label the decoder inputs $\left(\mathrm{IN}_{1}, \mathrm{IN}_{0}, \mathrm{EN}\right)$ and outputs (O0, O1, O2, O3).


Problem 2 (4 parts, 30 points)
Design Fiesta
Complete each design below. Be sure to label all signals.
Part A: Implement the following expression using N and
$P$ type switches. $\quad$ Out $_{x}=(\bar{A}+B \cdot \bar{C}) \cdot D$


Part B: Implement the following behavior using only pass gates and inverters.

$$
\begin{array}{ll|ll}
\mathrm{X} & \mathrm{Y} & \mathrm{Z} & \overline{\mathrm{Z}} \\
\hline \mathrm{~A} & 0 & \mathrm{Q}_{0} & \mathrm{Q}_{0} \\
\mathrm{~A} & 1 & \mathrm{~A} & \overline{\mathrm{~A}}
\end{array}
$$



Part C: Determine the appropriate expression for this mixed logic design. How many transistors are required?


Out $=\overline{A+\bar{B}}+\bar{C}+\bar{D} \cdot E$
$\#$ transistors $=8+6+4+4 \times 2=26 T$

Part D: Reimplement the design in Part C using only NAND and NOT gates. How many transistors are required?

\# transistors $=6+2 \times 4+2 \times 2=18 T$

Problem 3 (1 part, 25 points)
Assembly Programming
Part A (25 points) Complete this subroutine that searches an array of 100 integers beginning at memory address 5000 and returns its minimum (\$4) and maximum (\$5) values. Use the following registers: $\$ 1=$ array pointer, $\$ 2=$ end address, $\$ 3=$ current value, $\$ 6=$ branch predicate.

| label | instruction | comment |
| :--- | :--- | :--- |
| MinMax: | addi $\$ 1, \$ 0,5000$ | $\#$ init array ptr |
|  | addi $\$ 2, \$ 1,400$ | $\#$ set end address |
|  | lw $\$ 4, \quad(\$ 1)$ | $\#$ init min |
|  | add $\$ 5, \$ 3, \$ 0$ | $\#$ init max |
| Loop: | lw $\$ 3, \quad(\$ 1)$ | $\#$ load current element |
|  | slt $\$ 6, \$ 3, \$ 4$ | $\#$ if current >= min |
|  | beq $\$ 6, \$ 0$, Skip1 | $\#$ then skip update |
|  | add $\$ 4, \$ 3, \$ 0$ | $\#$ update min |
| Skip1: | slt $\$ 6, \$ 5, \$ 3$ | $\#$ if current <= max |
|  | beq $\$ 6, \$ 0$, Skip2 | $\#$ then skip update |
|  | add $\$ 5, \$ 3, \$ 0$ | $\#$ update max |
| Skip2: | addi $\$ 1, \$ 1,4$ | $\#$ point to next element |
|  | bne $\$ 1, \$ 2$, Loop | $\#$ if not done, loop |
|  | jr $\$ 31$ | $\#$ return to caller |

MIPS Instruction Set

| instruction | example | meaning |
| :---: | :---: | :---: |
| add | add \$1,\$2,\$3 | \$1 = \$2 + \$3 |
| subtract | sub \$1,\$2,\$3 | \$1 = \$2-\$3 |
| add immediate | addi \$1,\$2,100 | \$1 = \$2 + 100 |
| multiply | mul \$1,\$2,\$3 | \$1 = \$2 * \$3 |
| divide | div \$1,\$2,\$3 | \$1 = \$2 / \$3 |
| and | and \$1,\$2,\$3 | \$1 = \$2 \& \$3 |
| or | or \$1, \$2, \$3 | \$1 = \$2 \| \$3 |
| xor | xor \$1,\$2,\$3 | \$1 = \$2 xor \$3 |
| and immediate | andi \$1,\$2,100 | \$1 = \$2 \& 100 |
| or immediate | ori \$1,\$2,100 | \$1 = \$2 \| 100 |
| xor immediate | xori \$1,\$2,100 | \$1 = \$2 xor 100 |
| shift left logical | sll \$1,\$2,5 | \$1 = \$2 << 5 (logical) |
| shift right logical | srl \$1,\$2,5 | \$1 = \$2 >> 5 (logical) |
| shift left arithmetic | sla \$1,\$2,5 | \$1 = \$2 << 5 (arithmetic) |
| shift right arithmetic | sra \$1,\$2,5 | \$1 = \$2 >> 5 (arithmetic) |
| load word | 1w \$1, (\$2) | \$1 = memory [\$2] |
| store word | Sw \$1, (\$2) | memory [\$2] = \$1 |
| load upper immediate | lui \$1,100 | \$1 $=100 \times 2{ }^{16}$ |
| branch if equal | beq \$1,\$2,100 | if $(\$ 1=\$ 2), ~ P C=P C+4+(100 * 4)$ |
| branch if not equal | bne \$1,\$2,100 | if $(\$ 1 \neq \$ 2), ~ P C=P C+4+(100 * 4)$ |
| set if less than | slt \$1, \$2, \$3 | if (\$2 < \$3), \$1 = 1 else \$1 = 0 |
| set if less than immediate | slti \$1, \$2, 100 | if (\$2 < 100), \$1 = 1 else \$1 = 0 |
| jump | j 10000 | $\mathrm{PC}=10000$ |
| jump register | jr \$31 | PC = \$31 |
| jump and link | jal 10000 | \$31 = PC + 4; PC = 10000 |

Problem 4 (4 parts, 36 points)
"Math is fun"
Part A (9 points) Consider the instruction set architecture below with fields containing zeros.

| 00000000 | 000000 | 000000 | 000000000000000000 |
| :---: | :---: | :---: | :---: |
| opcode | dest. reg. | source 1 reg. | immediate value |

What is the maximum number of opcodes? 256
What is the number of registers?

| 256 |
| :---: |
| 64 |

What is the range of the signed immediate value? $\qquad$
Part B (9 points) For the eight bit representations below, determine the most positive value and the step size (difference between sequential values). All answers should be expressed in decimal notation. Fractions (e.g., 3/16ths) may be used. Signed representations are two's complement.

| representation | most positive value | step size |
| :---: | :---: | :---: |
| unsigned integer <br> ( 8 bits) . (0 bits) | 255 | 1 |
| signed fixed-point <br> ( 6 bits) . (2 bits) | 31 | $1 / 4$ |
| unsigned fixed-point <br> $(0$ bits) $)(8$ bits) | $255 / 256$ | $1 / 256$ |

Part C (6 points) A 48 bit floating point representation has a 37 bit mantissa field, a 10 bit exponent field, and one sign bit.

What is the largest value that can be represented (closest to infinity)?
What is the smallest value that can be represented (closest to zero)?
How many decimal significant figures are supported?
11
Part D (12 points) For each problem below, compute the operations using the rules of arithmetic, and indicate whether an overflow occurs assuming all numbers are expressed using a five bit unsigned fixed-point and five bit two's complement fixed-point representations.


Problem 5 (5 parts, 30 points)
Microcode in Reverse
The microcode fragment below comes from a color scanner control program that runs on the datapath discussed in class. Unfortunately, don't care values (X) have been converted to zeros. Assume register zero is a normal register (not hardwired to the value zero).

| $\#$ | $X$ | $Y$ | $Z$ | $r w e$ | im <br> en | im va | $a u$ <br> en | $-a / s$ | $l u$ <br> $e n$ | $l f$ | su <br> en | st | $l d$ <br> en | $s t$ <br> $e n$ | $r /-w$ | msel |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 3 | 1 | 1 | 4000 | 0 | 0 | 1 | C | 0 | 0 | 0 | 0 | 0 | 0 |
| 2 | 3 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 |
| 3 | 0 | 0 | 2 | 1 | 1 | FF | 0 | 0 | 1 | 8 | 0 | 0 | 0 | 0 | 0 | 0 |
| 4 | 0 | 0 | 0 | 1 | 1 | 8 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| 5 | 0 | 0 | 1 | 1 | 1 | FF | 0 | 0 | 1 | 8 | 0 | 0 | 0 | 0 | 0 | 0 |
| 6 | 1 | 2 | 2 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 7 | 0 | 0 | 0 | 1 | 1 | 8 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| 8 | 0 | 0 | 1 | 1 | 1 | FF | 0 | 0 | 1 | 8 | 0 | 0 | 0 | 0 | 0 | 0 |
| 9 | 1 | 2 | 2 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 10 | 0 | 0 | 0 | 1 | 1 | 8 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| 11 | 0 | 2 | 2 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 12 | 2 | 0 | 2 | 1 | 1 | 2 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 |
| 13 | 3 | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 |

Part A (5 points) Describe the operation that occurs during cycle 2. Be specific.

$$
\$ 0<- \text { mem[ } 0 \times 4000]
$$

## For the remaining parts, assume $\$ 0=0 \times 44022118$ at the end of cycle 2.

Part B (5 points) What is the value of register 0 at the completion of cycle 7 (in hexadecimal).
$0 \times 4402$
Part C (5 points) What is the value of register 2 at the completion of cycle 9 (in hexadecimal).
$0 \times 3 B$
Part D (5 points) What is the value of register 2 at the completion of cycle 12 (in hexadecimal).

## $0 \times 1 F$

Part E (10 points) Describe the operation of this microcode fragment. Be specific.
Four packed eight-bit unsigned integers are loaded from memory at 0x4000, unpacked. The average of the four values is computed and stored back to memory at $0 \times 4000$.

