#### Problem 1: (20 points)

Write a Boolean expression for each of these gate schematics.



#### Problem 2: (10 points)

A design team created the following logic expression for a project:

$$X = \overline{\overline{A + B \cdot C}} + A \cdot D \cdot \overline{\overline{E}} + F \cdot G$$

That logic is correct, but at the last minute, the customer added a new requirement:

"Add a new input H. If <u>H is low</u>, output <u>X must be low</u>, otherwise use the same logic as before"

Make the simplest change possible to add the required behavior. You're welcome to either write a new expression, or just describe what you would do.

AND the whole thing with H

### Problem 3: (25 points)

Implement the following Boolean expression in proper CMOS (N-FETs and P-FETs). Assume that inputs and their complements are available (i.e. you may use something like  $\overline{C}$  as an input to a FET if needed).

$$F = \overline{(\overline{A} \bullet (\overline{B} + C))} + D$$

Derive expressions for the pull-up and pull-down switch networks (p.u. and p.d.) here:

Draw CMOS here:

$$pu = F = A + B \cdot C + D$$

p.u. = \_\_\_\_\_

$$p\partial = F = \overline{A} \cdot (\overline{B} + C) \cdot \overline{D}$$
  
p.d. =  $\overline{A} \cdot (\overline{B} + C) \cdot \overline{D}$ 



# Problem 4: (20 points)

Manipulate the following mixed-logic schematic to implement it using only **ANDs** and **inverters**. The <u>same circuit</u> is repeated here twice <u>in case you ruin one</u>. Please <u>mark the one that you want graded</u>.



Mark here if you want this one graded.



 $\triangle$  Mark here if you want this one graded.

## Problem 5: (25 points)

Using the truth table below, create a K-map and solve for a minimal sum-of-products expression.

Α	В	С	D	Y
0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	0
0	1	0	0	1
0	1	0	1	0
0	1	1	0	1
0	1	1	1	0
1	0	0	0	1
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

Label the rows and columns of the K-map appropriately.



 $A = \frac{A \cdot B + C \cdot \overline{D}}{A \cdot B + A \cdot \overline{D}} + B \cdot \overline{D} + A \cdot \overline{D}$